

MECHANICAL VIBRATION MEASUREMENT  
EDWARD PATRICK APPERT  
1953

Library  
U. S. Naval Postgraduate School  
Monterey, California









## MECHANICAL VIBRATION MEASUREMENT

E. F. ALFERT

Library  
U. S. Naval Personnel School  
Anchorage, Alaska 99501



MECHANICAL PLASTIC MEASUREMENT

by

Edward Patrick Flynn  
Lieutenant, United States Navy

Submitted in partial fulfillment  
of the Requirements  
for the degree of  
MASTER OF SCIENCE  
in  
MECHANICAL ENGINEERING

United States Naval Postgraduate School  
Monterey, California  
1953

A58

This work is accepted as fulfilling  
the thesis requirements for the degree of  
MASTER OF SCIENCE  
in  
TECHNICAL ENGNERING  
from the  
United States Naval Postgraduate School.



## PREFACE

In the calibration of mechanical vibration pickup the accuracy of the calibration depends upon how accurately the displacement of the pickup can be measured.

This thesis has been a study into the feasibility of calibrating vibration pickups by means of an optical interferometer system. The unit used in the study was designed by Professor E. K. Catteau in 1952 and work was done by this author from January 1953 through May 1953 at the United States Naval Postgraduate School, Monterey, California.

The author is indebted to Professor Catteau for his valuable guidance throughout the entire work and to Professor C. H. Kalmback for his helpful assistance. Grateful acknowledgement is due to Joe Oktavec for the excellence of the machine work involved.



## TABLE OF CONTENTS

	Page
Certificate of Approval	i
Preface	ii
Table of Contents	iii
List of Illustrations	v
Table of Symbols and Abbreviations	vi
Chapter I Summary	1
1. Introduction	1
2. Objective of this Thesis	1
3. General Methods Employed	1
4. Findings	3
Chapter II Theory of Interferometer Operation	4
Chapter III Design Considerations and Changes Required	5
1. Original Unit	6
2. Mercury Light Source	6
3. Quartz Plates	7
4. Photoelectric Tube	10
Chapter IV Interpretation of the Results	12
1. Phototube Output	12
2. Accelerometer Output	12
3. Presentation of the Outputs	12
Chapter V Results	14
1. Test Runs	14
2. The Test Unit	14
3. Accelerometer Calibration	14



TABLE OF CONTENTS (CONT'D)

	Page
Chapter VI Conclusions	16
1. Feasibility of the Method	16
2. Suggestions for further study	16
Appendix I	17
Bibliography	21



## LIST OF ILLUSTRATIONS

	Page
Figure 1 Diagram of Interferometer unit	2
Figure 2 Fabry-Perot Interferometer	4
Figure 3 Haidinger fringe pattern	5
Figure 4 Haidinger fringe intensity contours	6
Figure 5 Intensity of Transmitted light	9
Figure 6 Standard spectral response, 3-4	11
Figure 7 Interferometer output	13
Figure 8 Test setup	18
Figure 9 Calibration unit	19
Figure 10 Oscillograph wave patterns	20



TABLE OF SYMBOLS AND ABBREVIATIONS

$d$  Distance between optical flats.

$n$  An integer greater than zero.

$\lambda$  Wavelength of light source.

$\varphi$  Angle of incidence or refraction.

$\text{Å}^0$  Angstrom units.  $1 \text{ Å}^0 = 10^{-8} \text{ cm.}$

$m$  Kilometers.

$a$  Acceleration of pickup in "g".

$\omega$  Frequency of vibration in radians per second.

$x$  Amplitude of vibration in inches.



## CHAPTER I

### SUMMARY

#### 1. Introduction.

An important consideration in the employment of a seismic pickup is the accuracy and reliability of the criteria set up to evaluate the response characteristics of the instrument.

In the calibration of any seismic pickup the accuracy of the calibration will be directly dependent on how accurately one knows and can describe the motion imparted to the pickup.

The methods generally employed for applying a known motion to the pickup are:

- (1) Mechanical Methods
- (2) Transfer Function Methods
- (3) Secondary Standard Methods.

The mechanical method and the transfer function method are adequate for calibrations over a narrow frequency range. Standard references are available delineating the limits of these methods.

#### 2. Objective of this thesis.

This thesis is an investigation into the use of an optical secondary standard of displacement for a seismic pickup, specifically as applied to the development of an accelerometer pickup.

#### 3. General Methods Employed.

Reference to figure 1 will show the schematic arrangement of the components employed in the test setup. These components include a mercury lamp, filters, a collimating lens, silvered optical flats, a condensing lens, a field stop, a photoelectric tube, and a means of visual presentation of the output of the phototube.



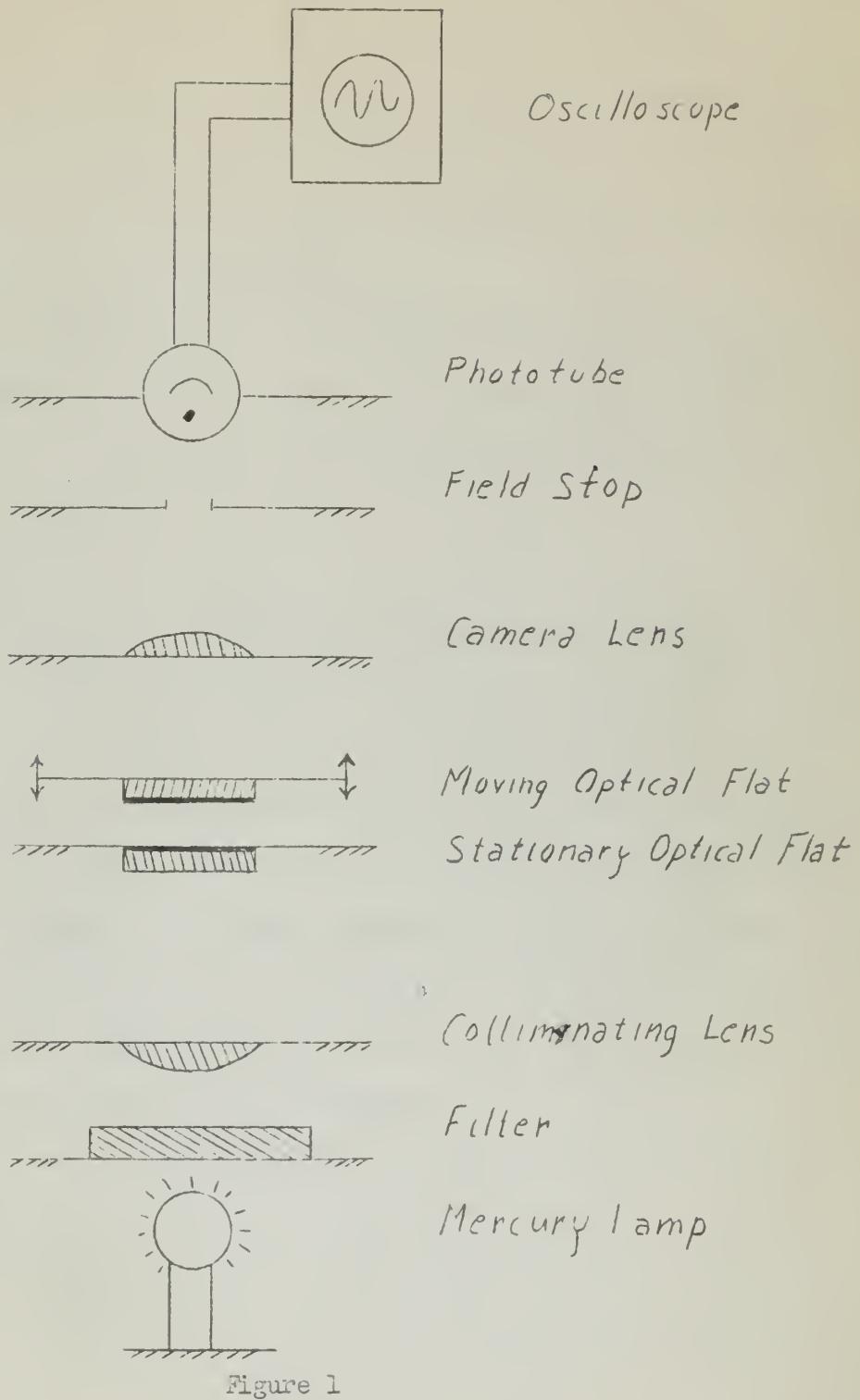


Figure 1



When the optical flats are made parallel (by external adjustments) the image of the extended source reflected in the air film between the two plane silvered flats produces the well known Haidinger fringes. A displacement of the optical flat by an amount equal to half a wavelength of the monochromatic light source will cause the central image of the fringe pattern to undergo one cyclic change as from dark to light. By proper adjustment of the optical stop and the photocube the change in the central dot will be recorded on the cathode ray oscilloscope.

In the test setup the moving optical flat is vibrated by an electromagnetic vibration inducer. The oscilloscope indicates the changes in the displacement of the optical flat per cycle of the vibration inducer.

#### 4. Findings.

The interferometer principles provide an excellent method of measuring displacements. In the calibration of pickups the calibration curve of the pickup and the amplitude response curve may be readily obtained. The apparatus is complex to build, but extremely stable once adjusted. The success of the unit is indicated by its ability to operate over a wide frequency and amplitude range.

Critical design features are the method of keeping the optical flats parallel during vibration of the moving flat, and maintaining the stationary flat without any motion.



CHAPTER II  
THEORY OF ETHER-THICKNESS METERS

The employment of Haidinger fringes in the Fabry-Perot interferometer is generally studied in an undergraduate course in optics. A brief review of the principle is given here to refresh the principles in the minds of the readers so that the design problems involved may be understood.

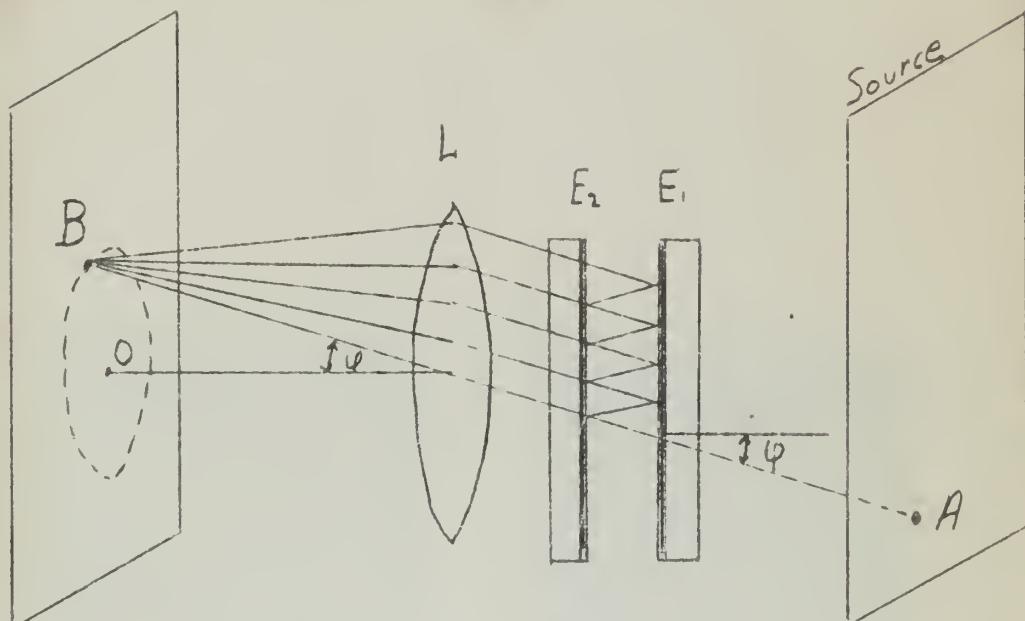


Figure 2

A monochromatic light ray from point  $A$  on the extended source transverses the silvered optical flats  $EE$ . Since the flats are parallel the multiple reflected emergent rays are all parallel to the direction of the incident ray. If the emergent beams are collected by lens  $L$ , they form at point  $B$  a part of a Haidinger fringe pattern.



The condition for reinforcement of the rays listed here in Fig 18:

$$2d \cos \varphi = m \lambda$$

This condition will yield a circle at the intersection of the rays of the lens with the screen. The circle diameters are proportional to the focal length of the image-forming lens and inversely as  $\sqrt{d}$ , where  $d$  is the separation of the two flats. Altering the distance between the flats by one-half the wavelength of the light source will cause the central image of the Fraunhofer fringes to complete one cycle of change of the light intensity (from light to dark in the case of figure 3).

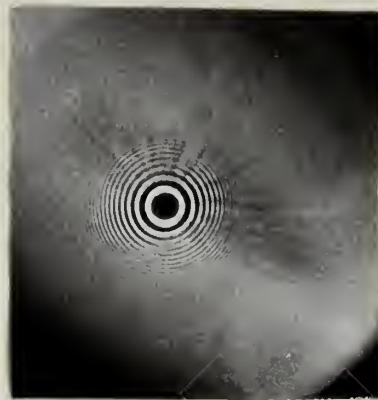


Figure 3



## CHAPTER III

### DESIGN CONSIDERATIONS AND CIRCUITS DESCRIBED

#### 1. Original Unit.

The unit as designed by Professor Cetromic consisted of: a Hanovia mercury light source, two quartz optical flats surfaced on the plane side with aluminum film, camera and collimating lenses of 38 mm focal length, a field stop and an RCA 1-1-42 vacuum photovoltaic tube. Reference to figure 1, page 2, shows the arrangement of the components.

This original unit failed to function properly for numerous reasons, each of which will be taken up under the heading of the component involved.

#### 2. Mercury Light Source.

The obvious choice for monochromatic light in Interferometry is the green light of the mercury arc with a wavelength of 5461 Å. The mercury light source is readily available as are the required filters to render the light almost perfectly monochromatic. These advantages outweigh the disadvantages of lowered intensity at higher frequencies and the reduced response of the crystal photovoltaic at this wavelength.

The operation of the Hanovia mercury light failed to operate satisfactorily. The ballasting of the high pressure design rapidly resulted in an introduced pressure broadening effect which caused the Maltinger fringe pattern to disappear. This problem was rectified by the purchase from the Rank Company of Pasadena, California of a special low pressure mercury light arranged in a



flat spiral. Care was taken in the design of the bulb that it could withstand any vibration forces that might be encountered in the calibration tests. A high intensity light is desired since the greater the intensity of the monochromatic light source the stronger the signal produced by the photoelectric tube. The space limitations of the calibration unit restricted the size of the R & M light to one of about 40 watts.

### 3. Quartz Flats.

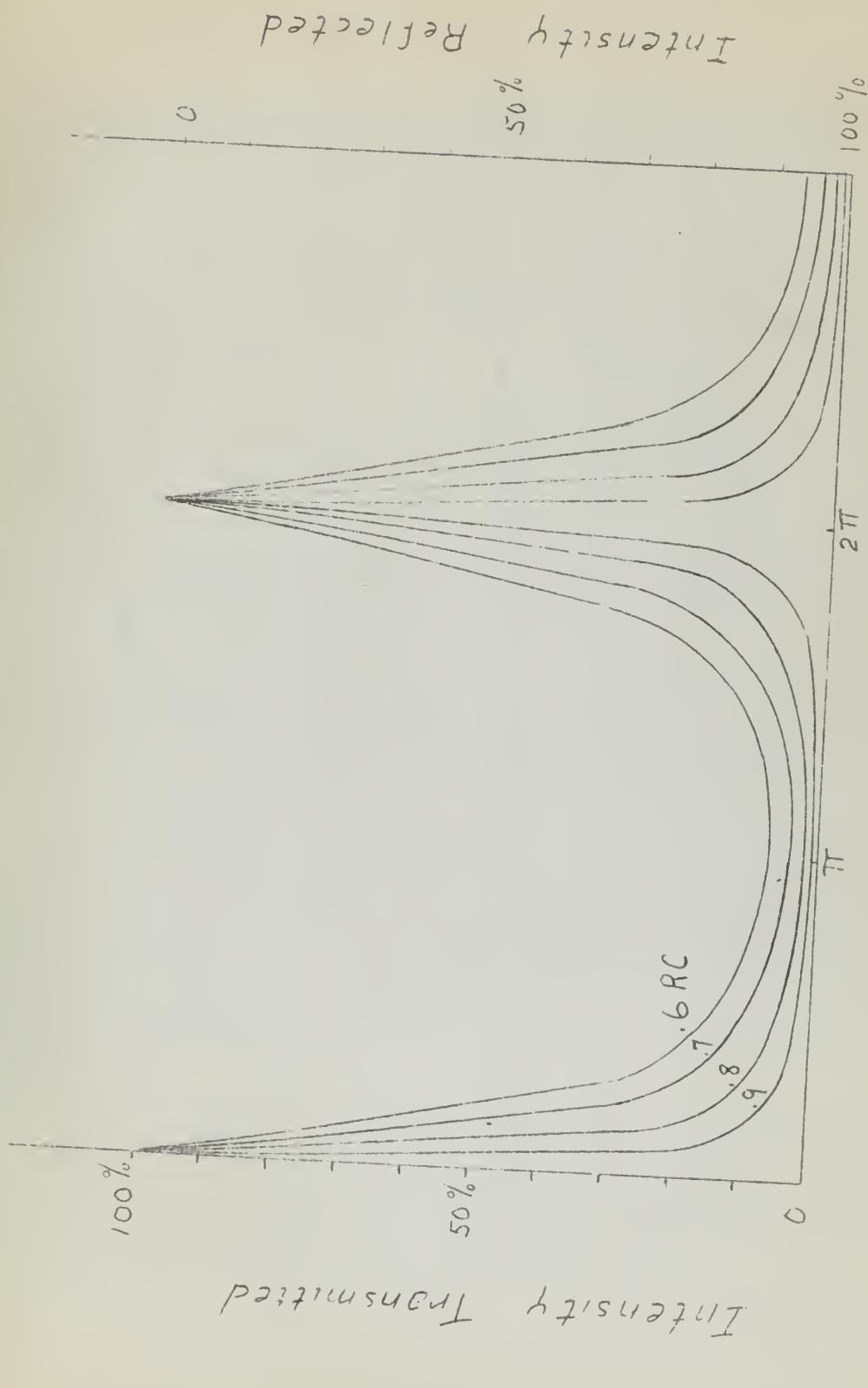
Three important design considerations are associated with the quartz flats, viz: the sharpness of the fringes observed, the intensity of the light which arrives at the phototube, and the size of the central image at the optical stop. The successful operation of the unit depends upon satisfying these highly critical and mutual dependent requirements.

The sharpness of the fringes (distribution of intensity) has been set in classical form by Kiry (Reference 3). In Figure 4 is shown the intensity contours for the Haidinger fringes, showing how their sharpness depends upon the reflecting power. When the mirror surfaces reflect between 20 to 50% of the incident light the bright fringes almost equal the incident light intensity, less absorption, while the dark fringes represent almost complete exclusion of the incident light.

As the reflecting coefficient approaches 100% the fringe sharpness improves, but the intensity of the light received by the phototube becomes too low to be effective. This consideration requires that the mutually contradictory factors of high reflection and high transmission be compromised. Figure 5 shows the relation



Figure 4





between the reflecting coefficient and fraction transmitted for both aluminum and silver films. A satisfactory compromise between figures 4 and 5 coupled with several experimental mirrors resulted in a 80% reflecting power coating as the most desirable for the unit involved.

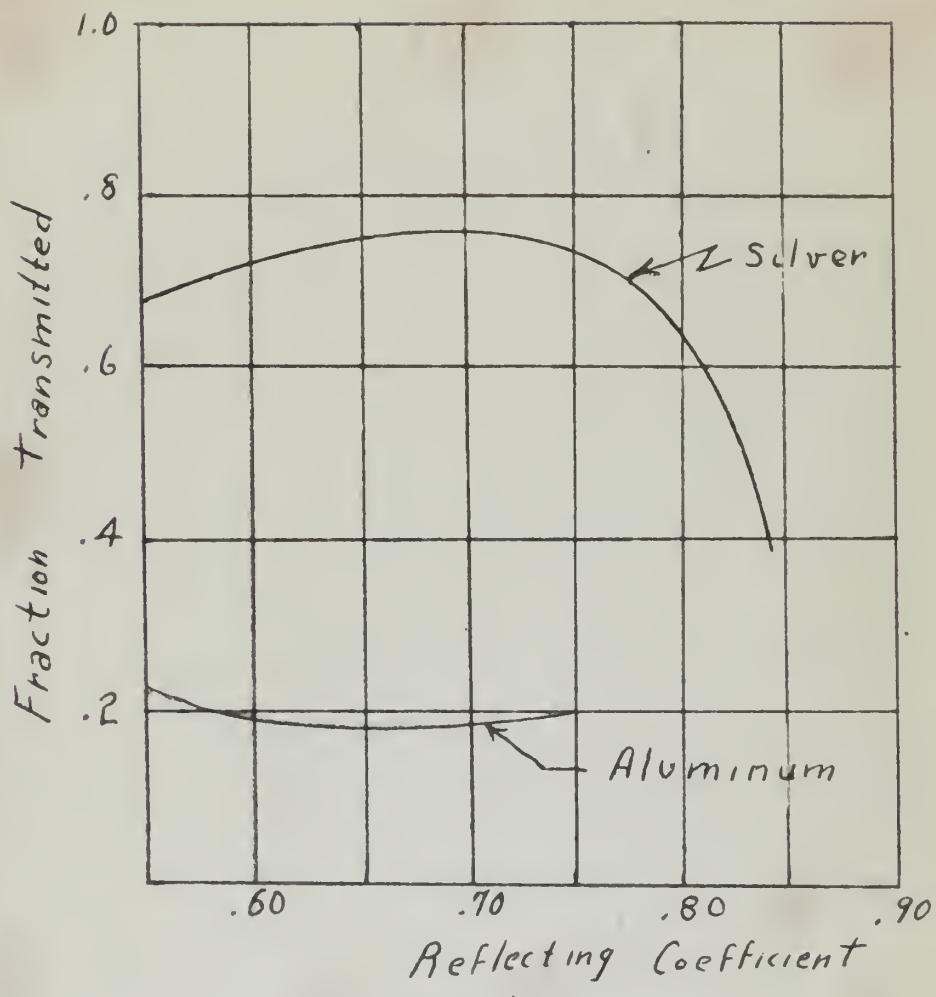


Figure 5

The original unit contained filters with aluminum mirrors. The power efficiency of the aluminum mirror as indicated by figure 5 dictated the change to the silver mirror.



The quartz flats were prepared for silvering by the ionic bombardment technique. The silvering was performed by evaporating the silver from a tungsten filament under a vacuum of about  $10^{-5}$  mm of Hg. To obtain optimum purity of the deposited silver there, reducing absorption losses required the preparation of a large number of mirrors before acceptable ones were obtained.

The distance between the optical flats (d) in the original unit was 0.286 inches. This produced a central image at the focus of the condensing lens with a diameter of about 0.015 inches. In order to increase the diameter of this image the distance between the optical flats was decreased to 0.150 inches, resulting in an increase in the central image to 0.018 inches. The moving optical flat was designed to vibrate with a maximum amplitude of 0.0075 inches, giving a 100% factor of safety before flats would collide.

#### 4. Photoclectric Tube.

The original unit was designed to utilize an RCA photoclectric tube 1-F-42. This tube was chosen for its response to the  $5461 \text{ \AA}$  mercury light and its desirable size. It is only about 1 inch in length by  $\frac{1}{4}$  inch in diameter with the photocathode at the end of its tubular structure. Figure 6 indicates the spectral response characteristics of the tube.

Reference again to figure 1 shows that the tube is required to pick up the light passed through the field stop and forward it to the recording instrument. The tube performed this specific function satisfactorily, and did transmit a signal indicating a change in the central image from a bright to a dark image. However, even after the change in the mercury light and to the optical



flats the intensity of the light which the phototube received resulted in a current flow of the order of  $10^{-10}$  amperes. This current flow was so low that it was difficult to distinguish between the noise of the electronic equipment and the signal output of the phototube. Since the unit as originally built left no room for a larger phototube, the entire physical structure of the assembly was changed to accommodate a photomultiplier tube.

The photomultiplier chosen, the RCA 141-21, has the same spectral response as the 1-1-42 (figure 6). This tube is capable of producing a maximum current amplification of 2,000,000 at an applied voltage of 100 volts per stage. Since amplification was now accomplished in the phototube, the reduction in the noise level resulted in a relatively low noise to signal ratio at the recording instrument.

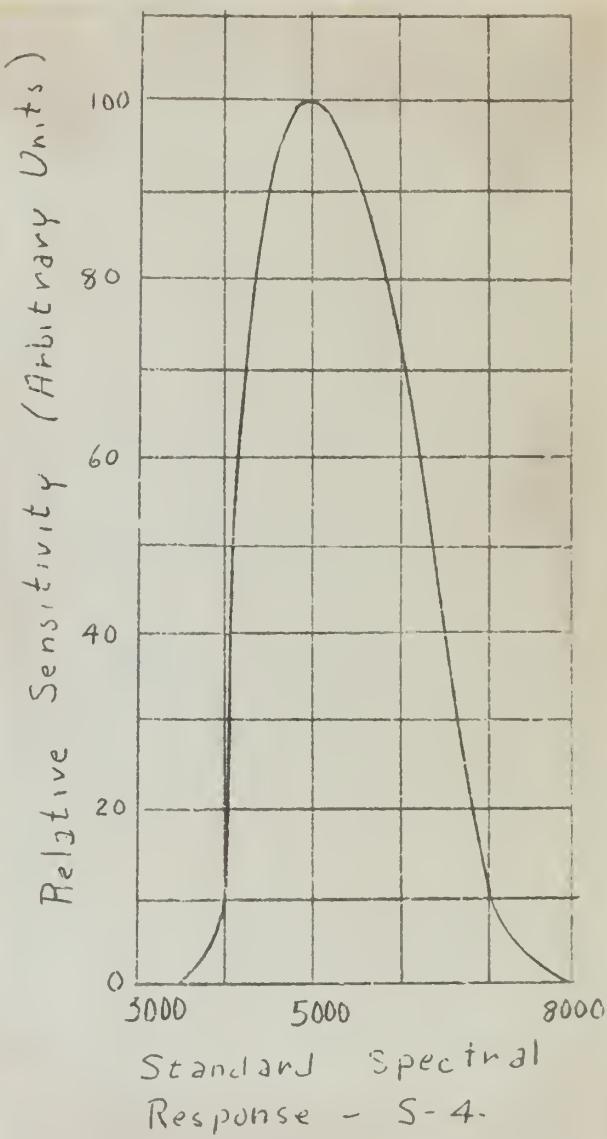


Figure 6



CHAPTER IV  
INTERPRETATION OF THE RESULTS

1. Phototube Output.

Each time the separation between the optical flats is changed by one-half of the wavelength of the mercury light source the central image of the Fraunhofer fringe completes one cyclic change. For the mercury line  $5461\text{\AA}$  this corresponds to a change of 0.00001071 inches in the separation of the plates. If the moving optical flat is vibrating at 1000 cycles per second through an amplitude of 0.0001 inches the phototube will be acted upon by a change in light cycles equal to

$$4 \times 1000 \frac{0.0001}{0.00001071} \quad \text{or} \quad 37055 \text{ cycles per second.}$$

2. Accelerometer Output.

If an accelerometer is attached in some manner to the moving optical flat this amplitude and frequency would correspond to an acceleration of:

$$1 \quad a = r \omega^2 = \frac{0.0001}{12} \times (1000 \times 2\pi)^2 = 3289$$

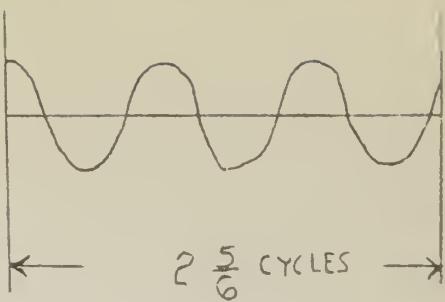
Correlation of the accelerometer output with the output of the phototube yields a true calibration for the acceleration of.

3. Presentation of the Outputs.

Figure 3 shows the test setup. The output of the phototube is displayed on the Y axis of the Cathode Ray Oscilloscope. When the time sweep of the oscilloscope is made equal to the one vibration of the unit, the number of peaks on the curve in one cycle will equal the number of changes in distance between the optical flats in units of half wave lengths of light. See figure 7.



this method one may immediately determine the amplitude of displacement occurring in an accelerometer which vibrates through the same displacement as the moving optical flat.



Interferometer Output

Figure 7



## CHAPTER V

### RESULTS

#### 1. Test Runs.

Figure 8 shows a composite of photographs taken during test runs. The runs were made at several frequencies and amplitudes of vibrations. The variation of the central image is super-imposed on a 60 cycle wave. By utilizing the 60 cycle wave as a time base, and knowing the frequency of vibration one may readily count the "pips" and ascertain the number of halfwave length changes in displacement between the optical flats.

Had a D.C. mercury light source been used the time base could be the frequency of the vibration. The photographs would then be as in figure 7. Lack of a 3000 volt D.C. supply voltage prevented the author from using this more direct approach.

#### 2. The Test Unit.

The unit used in this investigation easily complied with all the criteria by which we judge a measurement standard:

- a. It has a wide frequency and amplitude range.
- b. It is extremely stable as regards time, temperature and rugged use.
- c. It does not introduce any harmonic distortion.
- d. The output is related to the mechanical motion only.
- e. It is simple to use and easy to calibrate.

#### 3. Accelerometer Calibration:

The accelerometer calibration is obtained by recording the voltage across the bridge circuit of the transducer in the commercial type strain gage accelerometer. Calibration curves



obtained directly are: (1) amplitude of vibration vs. accelerometer output at constant frequency and (2) frequency vs. accelerometer output per "g". No calibration runs were actually made.



CHAPTER VI  
CONCLUSIONS

1. Feasibility of the Method.

The author is of the opinion that an optical standard for the measurement of small displacements can be successfully employed to calibrate seismic pickups to an accuracy of within one percent. (See appendix I). The unit used in the thesis work is extremely stable and capable of operation over a wide range of frequencies and amplitudes. As with any unit of a new design there are features which require further study and improvement to make the unit more than an experimental laboratory test piece. Of particular importance is to reduce the degree of mechanical coupling between the moving flat and the stationary flat, and to increase the intensity of the mercury lamp.

2. Suggestions for further study.

Improvements in the electronic arrangements for the calibration tests are a fertile field of study. The limitations of thesis time prevented building special circuits for measuring the outputs involved. Of great value in the calibration would be a circuit to record transient variations in the displacement and in the accelerometer output. The study of transient accelerometer measurements represents a field all too long neglected, and this unit coupled with an electron counting circuit would afford a convenient direct means of investigating the phenomenon.



## APPENDIX I

### ERROR CONSIDERATIONS

Assume the output of the phototube as shown by the scope is  $5 \frac{5}{6}$  cycles of a sine wave pattern. For mercury light of  $5461 \text{ \AA}$  the displacement of the plate is:  $5 \frac{5}{6} \times \frac{5461}{2}$  or  $26845 \text{ \AA}$ .

If the number of cycles on the scope is read to the nearest  $30^\circ$  the accuracy of the measurement is plus or minus  $1/24$  the oscilloscope cycle or  $114 \text{ \AA}$ .

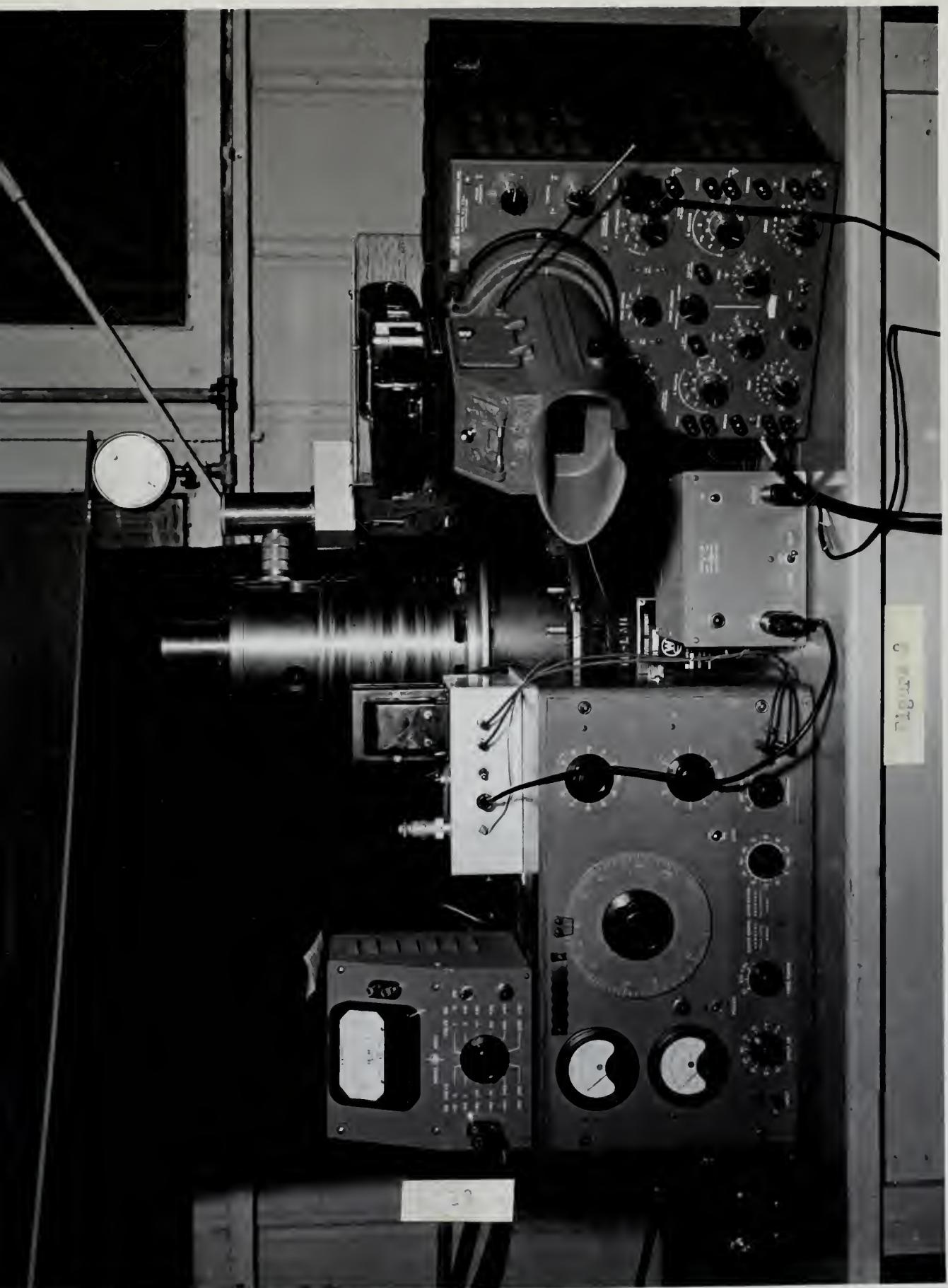
The error for this displacement (about .0001 inches) corresponds to:  $\frac{114}{26845}$  or  $0.42\%$ .

Obviously for smaller displacements the errors are larger and vice versa.

Another source of error is in the frequency measurements. There are available standards of frequency measurement accurate to within 0.1% or less, so that this error is almost negligible.

In actual work one might anticipate slightly higher errors, possibly due to slight vibrations of stationary optical flat. However, it is not anticipated that the error would total more than 1% in any measurement made.





OFFICIAL PHOTOGRAPH  
NOT TO BE USED FOR PUBLICATION  
BY ORDER OF  
THE CHIEF OF NAVAL OPERATIONS





## BIBLIOGRAPHY

1. Den Hartog, J.P. *Mechanical Vibrations*. New York, McGraw-Hill. 1947.
2. Tolansky, S. *Multiple Beam Interferometry*. London, Oxford University Press. 1948.
3. Jenkins, F.A. and White, R.E. *Fundamentals of Optics*. New York, McGraw-Hill. 1950.
4. Zworykin, V.K. and Rutherford, E.G. *Motoelectricity and its Application*. New York, John Wiley & Sons, Inc. 1945.
5. Hunt, A. *High Frequency Measurements*. New York, McGraw-Hill. 1951.
6. Tolansky, S. *Negative Dispersion Spectroscopy*. New York, Pergamon Publishing Corporation. 1947.
7. Indicators for Light Operated Relays, Light Measurements, Sound Reception. McGraw-Hill Corporation of America. 1945.
8. Dicker, F.J. *Measurement of Small High Frequency Vibration Beam Amplitudes by Interferometer Principles*. U.S. Naval Postgraduate School, Monterey, Calif. 1951.















JUL 2  
JUL 3  
JUL 4  
AUG 10  
FEB 1  
FEB 15  
MAR 1

BINDERY  
312  
RENEWED  
RENEWED  
RENEWED  
RENEWED  
RENEWED

20650  
Thesis Appert  
A58 Mechanical vibration mea-  
surement.

DEC 17 '53  
FEB 1  
FEB 15  
MAR 1  
MAR 15

BINDERY  
312  
RENEWED  
RENEWED  
RENEWED  
RENEWED

20650  
Thesis Appert  
A58 Mechanical vibration measurement.

Library  
U. S. Naval Postgraduate School  
Monterey, California



thesA58  
Mechanical vibration measurement.



3 2768 002 01213 0  
DUDLEY KNOX LIBRARY